

Class 9 Maths Chapter 14 Statistics Ex 14.4

Question 1.

The following number of goals were scored by a team in a series of 10 matches
2, 3, 4, 5, 0, 1, 3, 3, 4, 3.

Find the mean, median and mode of these scores.

Solution:

To find the mean :

Here, $n = 10$

$$\begin{aligned}\therefore \bar{X} &= \frac{\sum_{i=1}^{n=10} x_i}{n} \\ &= \frac{2 + 3 + 4 + 5 + 0 + 1 + 3 + 3 + 4 + 3}{10} \\ &= \frac{28}{10} = 2.8\end{aligned}$$

Thus, mean = 2.8

To find median:

Now arranging the given data in ascending order,
we have 0, 1, 2, 3, 3, 3, 3, 4, 4, 5

$\therefore n = 10$, an even number

$$\begin{aligned}\therefore \text{Median} &= \frac{\left[\left(\frac{n}{2} \right)^{\text{th}} \text{ term} + \left(\frac{n}{2} + 1 \right)^{\text{th}} \text{ term} \right]}{2} \\ &= \frac{\left[\left(\frac{10}{2} \right)^{\text{th}} \text{ term} + \left(\frac{10}{2} + 1 \right)^{\text{th}} \text{ term} \right]}{2} \\ &= \frac{[5^{\text{th}} \text{ term} + 6^{\text{th}} \text{ term}]}{2} = \frac{3 + 3}{2} = \frac{6}{2} = 3\end{aligned}$$

Thus, median = 3

To find mode:

In the given data, the observation 3 occurs 4 times,
i.e., maximum number of times.

Thus, mode = 3

Question 2.

In a mathematics test given to 15 students, the following marks (out of 100) are recorded

41, 39, 48, 52, 46, 62, 54, 40, 96, 52, 98, 40, 42, 52, 60

Find the mean, median and mode of this data.

Solution:

To find the mean:

Here, $n = 15$

$$\begin{aligned}\text{As, } \bar{X} &= \frac{\sum_{i=1}^{n=15} x_i}{n} \\ &= \frac{[41 + 39 + 48 + 52 + 46 + 62 + 54 + 40 + 96 + 52 + 98 + 40 + 42 + 52 + 60]}{15} \\ &= \frac{822}{15} = 54.8\end{aligned}$$

Thus, mean = 54.8

To find median:

Arranging the given data in ascending order,
we have

39, 40, 40, 41, 42, 46, 48, 52, 52, 52, 54, 60, 62, 96, 98

$\therefore n = 15$, an odd number

$$\begin{aligned}\therefore \text{Median} &= \left(\frac{n+1}{2}\right)^{\text{th}} \text{ term} \\ &= \left(\frac{15+1}{2}\right)^{\text{th}} \text{ term} = \left(\frac{16}{2}\right)^{\text{th}} \text{ term} \\ &= 8^{\text{th}} \text{ term} = 52\end{aligned}$$

Thus, median = 52

To find mode:

In the given data, the observation 52 occurs 3 times,
i.e., the maximum number of times.

Thus, mode = 52

Question-3 The following observations have been arranged in ascending order. If the median of the data is 63, find the value of x.

29, 32, 48, 50, x, x + 2, 72, 78, 84, 95

Solution:

Here, the given observations are in ascending order.

Since, $n = 10$ (an even number)

$$\begin{aligned}\therefore \text{Median} &= \frac{\left[\left(\frac{n}{2} \right)^{\text{th}} \text{ observation} + \left(\frac{n}{2} + 1 \right)^{\text{th}} \text{ observation} \right]}{2} \\ &= \frac{\left[\left(\frac{10}{2} \right)^{\text{th}} \text{ observation} + \left(\frac{10}{2} + 1 \right)^{\text{th}} \text{ observation} \right]}{2} \\ &= \frac{[5^{\text{th}} \text{ observation} + 6^{\text{th}} \text{ observation}]}{2} \\ &= \frac{x + (x + 2)}{2} = \frac{2x + 2}{2} = x + 1\end{aligned}$$

Since, median = 63 [Given]

$$\therefore x + 1 = 63 \Rightarrow x = 63 - 1 = 62$$

Thus, the required value of x is 62.