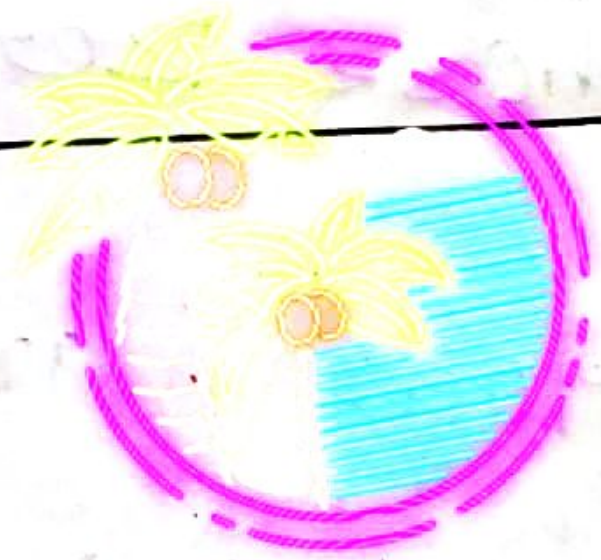


11.

PRACTICE - TIME.



Exam Based Questions:

Q.1. Find the Value for k for which $x^4 + 10x^3 + 25x^2 + 15x + k$ and ~~given number~~ exactly divisible by $x+7$.

Solⁿ:

Let

$$f(x) = x^4 + 10x^3 + 25x^2 + 15x + k$$

and $g(x) = x + 7$

Since $f(x)$ exactly divisible by $g(x)$

$$\therefore r(x) = 0$$

now,

$$\begin{array}{r} x^3 + 3x^2 + 4x - 13 \\ x+7 \overline{) x^4 + 10x^3 + 25x^2 + 15x + k} \\ \underline{x^4 + 7x^3} \\ 3x^3 + 25x^2 \\ \underline{3x^3 + 21x^2} \\ 4x^2 + 15x \\ \underline{4x^2 + 28x} \\ -13x + k \\ \underline{-13x - 91} \\ k + 91 \end{array}$$

$$\therefore k + 91 = 0$$

$$\boxed{k = -91}$$

$$(\alpha - \beta)^2 = 144$$

$$\text{Let } p(x) = x^2 + px + 45$$

$$\alpha + \beta = -\frac{b}{a} = \frac{-p}{1} = -p$$

$$\alpha\beta = \frac{c}{a} = \frac{45}{1} = 45$$

Now

$$(\alpha - \beta)^2 = 144$$

$$\Rightarrow (\alpha + \beta)^2 - 4\alpha\beta = 144$$

$$\Rightarrow (-p)^2 - 4(45) = 144$$

$$\Rightarrow p^2 - 180 = 144$$

$$\Rightarrow p^2 = 144 + 180$$

$$\Rightarrow p^2 = 324 \therefore p = \pm 18$$

$$\text{So, } p = \pm 18.$$

Q.2. If two zeros of the polynomial $f(x) = x^4 - 6x^3 - 26x^2 + 138x - 35$

are $2 \pm \sqrt{3}$. Find the other zeroes.

[Other zeroes are 7 & -5].

Q.3. If the squared difference of the zeros of the quadratic polynomial $x^2 + px + 45$ is equal to 144, find the value of p .

Solⁿ: Let two zeros are α & β where $\alpha > \beta$.

According to given condition

Q.4. Form a quadratic polynomial whose zeroes are $\frac{2}{3}$ and $-\frac{1}{3}$.

Q.5. If -1 is a zero of the polynomial $f(x) = x^2 - 7x - 8$, then find the other zero.

Q. Short question - (1 mark).

(i) The graph of $y = ax^2 + bx + c$,
where $a > 0$ is a _____,
opening _____.

(ii) The graph of $y = ax^2 + bx + c$,
where $a < 0$ is a parabola,
opening _____.

(iii) Write a quadratic polynomial
whose zeros are 5 and -3. ~~is~~

(iv) How many polynomials are
there having 4 and -2 as zeros?

(v) If one zero of the quadratic polynomial $(k-1)x^2 + kx + 1$ is -4 , then the value of k is?

(vi) If the sum of the zeros of the quadratic polynomial $kx^2 + 2x + 3k$ is equal to the product of its zeros, then $k = ?$

(vii) If α, β are the zeros of the polynomial $ax^2 + bx + c$, then $(\alpha^2 + \beta^2) = ?$

(viii) ~~of~~ on dividing a polynomial $p(x)$ by a non-zero polynomial $q(x)$, let $g(x)$ be the quotient and $r(x)$

be the remainder, then

$$P(x) = q(x) \cdot g(x) + r(x), \text{ where}$$

(a) $r(x) = 0$ always.

(b) $\deg r(x) < \deg g(x)$ always.

(c) either $r(x) = 0$ or $\deg r(x) < \deg g(x)$

(d) $r(x) = g(x)$.

(ix) If the zeros of a quadratic polynomial $ax^2 + bx + c$ are both negative, then a, b, c will have the same sign. (True/False).

(x) If α and β are the zeros of a quadratic polynomial $P(x)$, then $P(x) = \{x^2 - (\dots)x + \dots\}$,

